

Warm-Up:

Solve the following equations for the variable.

1)  $2w - 10 = 5w - 7$

$$\begin{array}{r} -2w \quad -2w \\ -10 = 5w - 7 \\ +7 \quad +7 \\ -3 = 3w \\ \frac{-3}{3} = \frac{3w}{3} \\ \boxed{w = -1} \end{array}$$

2)  $\frac{x}{4} = \frac{13}{2}$

$$\frac{52 = 2x}{2} \quad \boxed{x = 26}$$

3)  $7 + 2(y + 1) = 2y + 9$

$$\begin{array}{r} 7 + 2(y + 1) = 2y + 9 \\ 7 + 2y + 2 = 2y + 9 \\ 9 + 2y = 2y + 9 \\ 9 = 9 \end{array}$$

inf. many solutions

36, 30, 34

30)  $n = 1st \text{ integer}$   
 $n+2 = 2nd \text{ integer}$   
 $n+4 = 3rd \text{ integer}$

$$3(n+4) = 2n + 38$$

$$\frac{3n + 12 = 2n + 38}{-2n \quad -2n}$$

$$\frac{n + 12 = 38}{-12 \quad -12}$$

$$n = 26$$

$\boxed{26, 28, 30}$

34)  $-3(2n - 5) = 0.5(-12n + 30)$

$$-6n + 15 = -6n + 15$$

Inf. Many Solutions

36) nail length =  $1 + \frac{1}{4}(x - 2)$

$$2\frac{1}{2} = 1 + \frac{1}{4}(x - 2)$$

$$\frac{5}{2} = 1 + \frac{1}{4}x - \frac{1}{2}$$

$$\frac{5}{2} = \frac{1}{4}x + \frac{1}{2}$$

$$\frac{4(2) - 4(\frac{1}{4}x)}{4}$$

$$8 = x$$

$\boxed{8\text{-penny nail}}$

## Section 2-6: Ratios and Proportions

A **ratio** is a comparison of two numbers through division.

Ratios can be expressed several ways.

$$x \text{ to } y \quad x:y \quad \frac{x}{y}$$

Whenever two ratios are equal to each other, it is called a **proportion**.

In a proportion, the cross products are equal to each other.

$$\frac{a}{b} = \frac{c}{d} \quad \text{so,} \quad ad = bc$$

Examples:

1) Determine whether the following ratios determine a proportion.

$$\frac{7}{8} \rightarrow \frac{49}{56}$$

Yes

$$392 = 392$$

Use cross products to determine whether each pair of ratios forms a proportion.

$$2) \frac{0.25}{0.6} \rightarrow \frac{1.25}{2}$$

No

$$.5 \neq .75$$

$$3) \frac{4}{5} = \frac{16}{20}$$

Yes

$$80 = 80$$

Examples:

4) Solve the proportion

$$\frac{n}{12} = \frac{3}{8}$$

$$\frac{8n}{8} = \frac{36}{8}$$
$$n = \frac{9}{2}$$

When two different measurements are put into a ratio, the result is a **rate**.

A ratio used to compare a size of a model to the actual size of an object is called a **scale**.

Examples:

5) The gear on a bicycle is 8:5. This means that for every 8 turns of the pedals, the wheels go around 5 times. Suppose the bicycle wheel turns about 2435 times during a trip. How many times would you have to crank the pedals during the trip?

8 pedal turns : 5 wheel turns

$$\frac{n}{8} \times \frac{2435}{5}$$

$$\frac{5n}{5} = \frac{19480}{5}$$

$$\frac{8}{5} \times \frac{n}{2435}$$

$$n = 3896$$

pedal turns

Examples:

6) In a road atlas, the scale for the map of Connecticut is 5 inches = 41 miles. The scale for the map of Texas is 5 inches = 144 miles. What are the distances represented by 2 1/2 inches on each map?

$$\frac{5}{41} = \frac{2\frac{1}{2}}{CT}$$

$$CT = 20.5$$

Mi

$$\frac{5}{144} = \frac{2\frac{1}{2}}{TX}$$

$$TX = 72$$

mi

Homework: pg. 109-110 #10-26 even, 27-30 all,  
32, 38, 41, 42

Section 2-6 Vocab